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BLOOM'S TAXONOMY REVISED ASPECT ON VISUALIZER AND VERBALIZER'S PROBLEM SOLVING

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## Abstract

The ability to solve problems is a part of learning mathematics that is very important. Problem solving prefers the processes and strategies undertaken by students in solving problems rather than results. The concept of learning corresponds to the stages in the bloom's taxonomy revised. The Bloom's Taxonomy revised has two dimensions, namely the dimensions of the cognitive process and the knowledge dimension. The knowledge dimension has four categories, but this research is only limited to procedural knowledge. The dimensions of cognitive processes are categorized into six types, namely remembering, understanding, applying, analyzing, evaluating, and creating. Learning implementation emphasizes the role of students. In addition, implementation must be balanced with the appropriate tools. In this study, the tools used were open-ended problems. This study aims to provide an overview of how open ended problem can help improve students' mathematical abilities through a Bloom's Taxonomy revised. The results of the study stated that students with visualizer cognitive style had more effective and efficient steps in solving problems well. It shows how it can create a problem from the open ended problem that is given. This can be a teacher's consideration in teaching, so that students can get the open ended problem. **Keywords:** Problem Solving, Bloom's Taxonomy Revised, Visualizer, Verbalizer.

## **INTRODUCTION**

Education is basically an effort to provide certain knowledge, insight, skills and expertise to humans to develop their talents and personalities. Education is also an activity that aims to improve one's abilities in various aspects including knowledge, skills, and attitudes (Hasibuan in Yanti, 2009). In the current reality of education, improving students' mathematical skills or skills is rarely done in school learning. Teachers not only teach mathematics as a tool, but teach mathematics as a human activity (Soedjadi, 2007, 6-7). This is one of the factors that causes some students to have a negative impression on mathematics (Sudarman, 2008 (a)), for example: mathematics is considered a scary thing (Lea Pamungkas, 2009), mathematics is difficult and boring (Becker and Schneider, 2009), mathematics is not fun (Zainurie, 2009). There are things that need to be done besides teaching memorized mathematics by using routine problems or closed problems, namely teaching mathematics lessons using open-ended problems, where the basis of open-ended problems are classified into three types, namely, 1) Process is open, 2) End product are open, and 3) ways to develop are open. This Open-ended problem will be adjusted to the content that is in the bloom's taxonomy revised of cognitive processes. This

can measure how much students are able to solve a problem

The most widely used methods for high-level expertise are Bloom's Taxonomy Revisedfor Educational Purposes. Bloom's Taxonomy Revised uses a multi-tiered scale for expertise needed for each measured student outcome. Organizing student results that are appropriate for the class. One of the aims of Bloom's taxonomy Revised is the extent to which teachers want students to understand and use concepts, to show their skills, and to have values, attitudes, and interests that they will have in society.

There are three types of taxonomy. the use of all three will be tailored to student learning outcomes and learning objectives. There are goals based on knowledge, goals based on expertise, and affective goals (affective: values, attitudes, and interests); accordingly, there is a taxonomy for each. Within each taxonomy, the skill level is permitted. Good student learning outcomes will determine when they are faced with a problem.

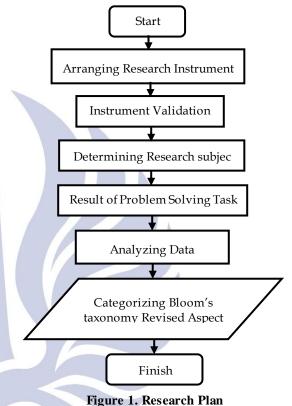
This objection focus on student's answer sheet. Certainly, this objection cant describe all of the way verbalizer or visualize do in general. But at least this can be seen as an open ended problem, which means that it can address students to find the solution with bloom's taxonomy revised content. However it can help the teacher to reconsidered to use the open ended problem as the main problem to measure the ability of cognitive students to solve a problem.

This discussion is based on cognitive process according to bloom's taxonomy revised, but there are some merge points to make it easier to understand where the content stands for. Indeed, this content is also has its own characteristic. The conceptual framework (table 1) in analyzing and categorizing adapted in students' answer sheet is based on the following format and content proposed by bloom's taxonomy revised. They are : and spatial visualizer. Object visualizer considered on whole object as main aspect of their answer and spatial visualizer considered on partial portion of the answer, so their answer more details. The problem was adapted from game in early 20's, It was about several people who try to cross a river with some kind of rule and the student's job is determine how many trip they did. The problem is also changed into open – ended problem, so it has multiple correct answer. The problem has been validated by highly competent in mathematics (Figure 1).

Tabel 1.Cognitive	abel 1.Cognitive Process of Bloom's Taxonomy Revised		
Levels	Descriptions		
Remembering	Retrieving, recognizing, and recalling relevant knowledge from long-term memory. This level is simply remembering or recalling previous learned information.		
Understanding	Constructing meaning from oral, written, and graphic messages through interpreting, exemplifying, classifying, summarizing, inferring, comparing, and explaining. This is essentially demonstrating understanding of information by explaining ideas or concepts		
Applying	Carrying out or using a procedure through executing, or implementing. Basically, this is using the information in another familiar situation		
Analyzing	Breaking material into constituent parts, determining how the parts relate to one another and to an overall structure or purpose through differentiating, organizing, and attributing		
Evaluating	Making judgments based on criteria and standards through checking and critiquing. This includes justifying a decision or course of action.		
Creating	Putting elements together to form a coherent or functional whole; reorganizing elements into a new pattern or structure through generating, planning, or producing. This includes generating new ideas, products, or ways of viewing things.		

## METHODS

The Student's worksheet used in this analysis is the visualizer and verbalizer student's worksheet. In detail, visualizer is devided by 2 part, there are object visualizer



#### **RESULT AND DISCCUSION**

In general, this topic is about algebra's riddle. The analyzed parts are defined as categorized Bloom's taxonomy revised. In fact, those parts rarely mention explicitly on how this classify into taxonomy. Using the format and content Categorization from Bloom's taxonomy revised, we can conclude that there are categories on some merge points on subject's results. They are visualizer and verbalizer subject aspect on remember and understand the problem, apply and analyze the solution through the problem, evaluate their answer, Creating a new problem with those new solution, and each indicator to make easier in categorize it.

#### 1. Object Visualizer

The object of the object visualizer was students of high school in Sidoarjo. This subject participated in the work of two Problem solving tasks and two interviews. In the first problem solving task, VO took 35 minutes, then an interview was conducted out. In the second problem solving task, it took 37 minutes, then an interview was conducted. This aims to observe whether the subject is consistent with the steps to solving the problems that were carried out previously.

		r Object Description
Content	Indicators	Details
	Read given problem	Subject reads the questions given.
Where the students remember and understand the problem	List the information	Subject writes down the informations known on the answer sheet
	List the question Sketch the problem	Subject deafers what he wants to find Subject illustrated the problem given. It seems like VO makes a
	-	kind of trip that can be done by the boat.
How students apply and analyze the	Make a map showing interrelation ships	Subject describes the model of a boat trip. It is seen that there are boats and the flow of travel from the boat. There are a number of adults and the number of teenagers is on the riverbank. Then Subject arranges a boat crossing by following the conditions / conditions provided.
analyze the solution through the problem	Construct a sketch to organize data Solve a problem	Subject constructs boat trips by following the rules that a boat can carry only 1 adult or 1 teenager or 2 teenagers. Subject try to find the solution by calculating the trip of boat do.
		And then, subject find those solution
How the student evaluate their answer	Check the answer	Subject revealed that the answer was correct. When subject states this, it does so by reviewing the answers he has written on the answer sheet. Subject occasionally looks at questions to check for errors that occur during the problem solving process. In addition, he also adjusted to the plan he had compiled beforehand.
	Try another strategy to solve the problems	Subject revealed that there were other alternative solutions. Subject uses the formula that he has found. Subject revealed that he found the formula from the two comparisons drawn.
Creating a new problem with those new solution	Creating a new solution from edited problem	Subject shows there are 2 answers, namely by changing the ratio of the number of adults and adolescents.

Table 1. Visualizer Object Description

Based on the analysis described above the object visualizer is able to solve the mathematical problem given. The work shown is related to the 4 stages of problem solving, (1) Understanding the problem; (2) Select or determine plans; (3) Carry out the plan; and (4) Evaluating results. The results of the visualizer object work are in accordance with Paivio & Richardson (in Kozhevnikov et al., 2005) which reveals that visualizers mainly rely on imagery when trying to do cognitiverelated tasks. In solving subject problems visualizer objects prioritize using drawing strategies to explain them. The results shown by the subject visualizer object can solve the problem very well. The answer given is also true for the problem. This is not in accordance with that stated by Woolner (2004), saying there is a suspicion that students with cognitive visualizers might fail in school mathematics because of a mismatch between the cognitive styles they have and the dominance of teachers who teach verbally. In other words, the subject of visualizer objects is able to solve mathematical problems accurately and precisely according to Kozevnikhov (2005) Object visualizers tend to encode images as a whole as a unified perception that is processed thoroughly. They tend to be faster and more accurate in recognizing and remembering things.

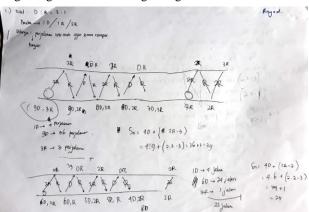


Figure 2. Visualizer Object's WorkSheet

## 2. Visualizer Spatial

Та	ble 2. Visualizer S	patial Description
Content	Indicators	Details
	Read given	Subject reads the questions
	problem	given.
	List the	Subject writes down the
Where the	information	informations known on the
students	A	answer sheet
remember	List the question	Subject deafers what he wants
and		to find
understand	Sketch the	Subject illustrates the situation
the	problem	the problem. Subject makes an
problem	•	illustration to clarify the
ieri y	burabay	situation the question so that it
y - 11 -	Julunu	makes it easier to find a
		solution.
	Make a map	Subject describes the model of
	showing	a boat trip. Subject seemed to
	interrelationships	make a boat trip to cross the
How		river with regard to the
students		requirements of the number of
apply and		people who could use the
analyze		boat. The subject also does the
the solution	Construct a	same for other comparisons.
		Subject constructs boat trips
through the	51101011 10	by following the rules that a
the	organize data	boat can carry only 1 adult or
problem	Solva a problem	1 teenager or 2 teenagers. Subject try to find the solution
	Solve a problem	by calculating the trip of boat
		do. And then, subject find
		uo. Anu men, subject miu

Content	Indicators	Details	related tasks	. More than that,
Content How the student evaluate their answer	Indicators Check the answer Try another strategy to solve the problems	Details those solution Subject revealed that the plan he did was correct and in accordance with what was planned. Subject also revealed that he had used things that were already known in the matter to work on the problem. When Subject states this, he does so by observing the answers he has written on the answer sheet. Subject occasionally looks at questions to check for errors that occur during the problem solving process. Subject revealed that there were other alternative solutions. Subject uses the formula that he has found. Subject revealed that he found the formula from the two comparisons drawn.	visualizer is because the work. This that spatial v analytically, to compile a The sp when lookin subject give able to fix i subject give subject also the subject also the subject also the subject and problem give saying there visualizers n mis match be	s. More than that, a more detailed the subject provides is in line with Kor visualizers tend to en- parts per section, and analyze each of patial visualizer such and analyze each of patial visualizer such and for solutions to s an inappropriate that the stage of en- s the correct answer gives 2 correct answer requires more time en. This is not in the is a suspicion that night fail in school etween the cognitive of teachers who teach
Creating a new	Creating a new solution from	Subject shows there are 2 answers, namely by changing	Content	Indicators Read given
problem with those	edited problem	the ratio of the number of adults and adolescents.		problem
new		addits and addrescents.	Where the	List the information
solution			Where the students	List the question
	\$ [] \ 1 = A:	innui: : AHI PRESTU II enga Inna Russi : Remoja	remember and understand	Sketch the
J. P.	5 A 6:2	r contrar projections by tibutured	the problem	problem
(1) r.	2 bring drangter dula. Lore. 1 ben hali be A. Araba dipa	y remain finned to B		
ke-	white he A means	I dewega be B armi fig		
	D premaja di A	+ deways fas,		Make a map
1	•	The use it . Iterity selen		showing
	Dirjetowen: 19 errory devect	= A heri = 24 her;		interrelationships
	Or w to 2 renja	= 1 +	_	
*	+ @   w	25 608,		
scien				
0	Bandingon q:3 Oike	femi : PINOPARSTV : Devise		
10、聚蛋野素 资素类素 素	Berner W W	· [ -] * Total +4 ×3 +3 = 39	How	urabav
P. \$ \$\$	vectores V 4	(a) the in firmer result	students	Construct
	Villian a land	Autor 112 Autor 112	apply and analyze the	Construct a sketch to
	× +   +   +   +   +   +   +   +   +   +	Untre 3:3 Parjokanni Avi +3	solution	organize data
Ridho.	Vx   0 - 1 0m	F	through the problem	Solve a problem
Figu	re 3. Visualizer S	Spatial's WorkSheet	Problem	Solve a problem

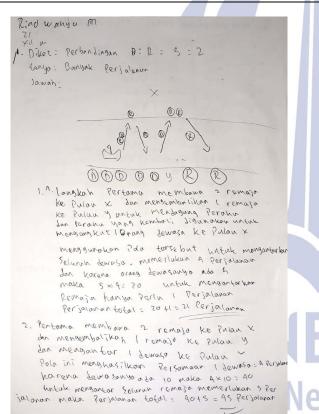
Based on the analysis described a visualizer spatial is able to solve the math problem given. The result related with the 4 problem solving, (1) Understanding the prol Select or determine plans; (3) Carry out the pla Evaluating. The results in line with Paivio & R (in Kozhevnikov et al., 2005) reveal that v mainly rely on imagery when trying to do

the subject of the spatial than the visualizer object information regarding his ozhevnikov (2005) stating encode and process images using spatial relationships f its components.

ubject experiences errors o problem number 1. The answer. But the subject is evaluating the results. The wer. The spatial visualizer swers to the problem. But e to find a solution to the line with Woolner (2004) at students with cognitive ol mathematics because of a ve styles they have and the ch verbally.

om the two	3. Verbali	zer	
/n.			
there are 2	Content	Indicators	Details
by changing number of		Read given	Subject reads the questions
cents.		problem List the	given.
ciits.		List the information	Subject writes down the informations known on the
	Where the	information	answer sheet
	students -	List the question	Subject deafers what he
_	remember	1	wants to find
in .	and -	Sketch the	Subject illustrates the
6 days	understand	problem	situation the problem. Subject
	the problem		makes an illustration to
			clarify the situation the
11			question so that it makes it
		and the second se	easier to find a solution.
		Make a map	There is one diagram given
Seleny		showing	by subject. But after being
		interrelationships	analyzed, the chart is only an
			illustration. Illustrations made
			by subject to the conditions
			of the questions given. Then
			VE provided information
			regarding the illustration he
			had made. Subject explained
			in detail in the form of a story
	aori S	urabay	about a trip carried out by adults and teen using a
	How	ulabay	concern.
ru uus.	apply and	Construct a	Subject constructs boat trips
	analyze the	sketch to	by following the rules that a
	solution	organize data	boat can carry only 1 adult or
	through the	organize data	1 teenager or 2 teenagers.
heet	problem	Solve a problem	Subject can find the
neet	1		connection of boat trips to the
			number of adults and
above the			teenagers. Subject found the
thematical			boat trip pattern. Subject
stages of			makes a pattern and find the
oblem; (2)			number of trips made by
an; and (4)			boats by changing the ratio of
Richardson			the number of adults and
visualizers			teenagers. Subject also writes
cognitive-			the formula related to the
			solution to this problem.

Content	Indicators	Details
Content		
	Check the	Subject corrects the work
	answer	done by re-reading the
		answer sheet. Subject also
		reread the question to make
		sure the answer he had done
How the		was correct.
student	Try another	Subject found the boat trip
evaluate	strategy to solve	pattern from the information
their answer	the problems	he had made. The travel
		pattern was expressed in the
		form of a formula, namely
		many trips is $4D + (2R-3)$ , D
		is the number of adults and R
		is the number of teenagers.
Creating a	Creating a new	Subject shows there are 2
new	solution from	answers, namely by changing
problem	edited problem	the ratio of the number of
with those		adults and adolescents.
new		
solution		



#### Figure 4. Verbalizer's WorkSheet

Based on the analysis described above the verbalizer is able to solve the mathematical problem given, the results shown by the verbalizer subject are in accordance with the 4 stages of problem solving, namely (1) Understanding the problem; (2) Select or determine plans; (3) Carry out the plan; and (4) Evaluating. The verbalizer subject is able to solve the problem given, even though there are indicators that are not met, namely rewriting the question on the question. The subject work of verbalizer in line with Paivio & Richardson (in Kozhevnikov et al., 2005) reveals that verbalizers rely primarily on verbal analysis strategies. This can be seen

in the answer of the subject in number 1. The subject of verbalizer is more comfortable in explaining using the words themselves through the information shown on the answer sheet. But when viewed from the work done by the subject of the verbalizer, the results shown are no better than the subject visualizer object. The work of the verbalizer subject looks inefficient when compared to the subject visualizer object. This is not in accordance with Riding and Agrell's (in Arnup et al. 2013) in his research entitled The effect of cognitive style and cognitive skill on school subject performance that results in students' cognitive-style verbalizers getting better results than students cognitive style visualizer in solving mathematical problems. However, if viewed from his work, the verbalizer subject is able to answer all the questions correctly.

## Closure

## Conclution

In Summary, integrating open—ended problem can make students explore their ability to solve a problem. While in this case, Bloom's taxonomy revised can make it easier to prove that there are some points that many teacher forgot that those ability that students' have must be force to appear by using open—ended problem. Even there are many difficulties to make this problem, at least in this case, the visualizer and verbalizer subject can explore their knowledge to finish well. Compared to those three subjects, they can give a different solution with kind of alternative problem solving with their characteristic. So, it can shows that there are three different cognitive style.

## Suggestion

Based on the conclusions above and the condition of the researcher during the field, the researcher gives the following suggestions:

- 1. The results of the study show that although all stages of problem solving appear on all three subjects, descriptors that show their problem solving characteristics have several differences. This difference affects the strategy of solving problems they take. Therefore, teachers should pay attention to the differences in the cognitive style of visualizer objects, spatial visualizers, and verbalizers in the learning process, especially in preparing learning that can involve or even improve student problem solving.
- 2. For educators, it is better to design and familiarize learning that encourages students to further optimize the ability to solve problems using open-ended problems.
- 3. For researchers who want to conduct research that is relevant to this study.
  - a. At the interview, the researcher should use a video recorder to record so that no data or events are

missed and the researcher is facilitated more easily when analyzing the data.

- b. The researcher should be able to distinguish different answers and different ways when analyzing the results of TPM work by the subject of the study, so that there are clear differences between the stages of problem solving.
- c. In general, problem solving assignments made by researchers must be able to collect student problem solving according to the cognitive style possessed by students.
- d. The subject of this study only focuses on students in cognitive visualizer objects, spatial visualizers, and verbalizers without looking at gender. So, in the next study it is expected to see gender in determining the subject of research can be represented.

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